



Lakes & Watersheds ***Measurements & Modeling***

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Lake Leaders 2018

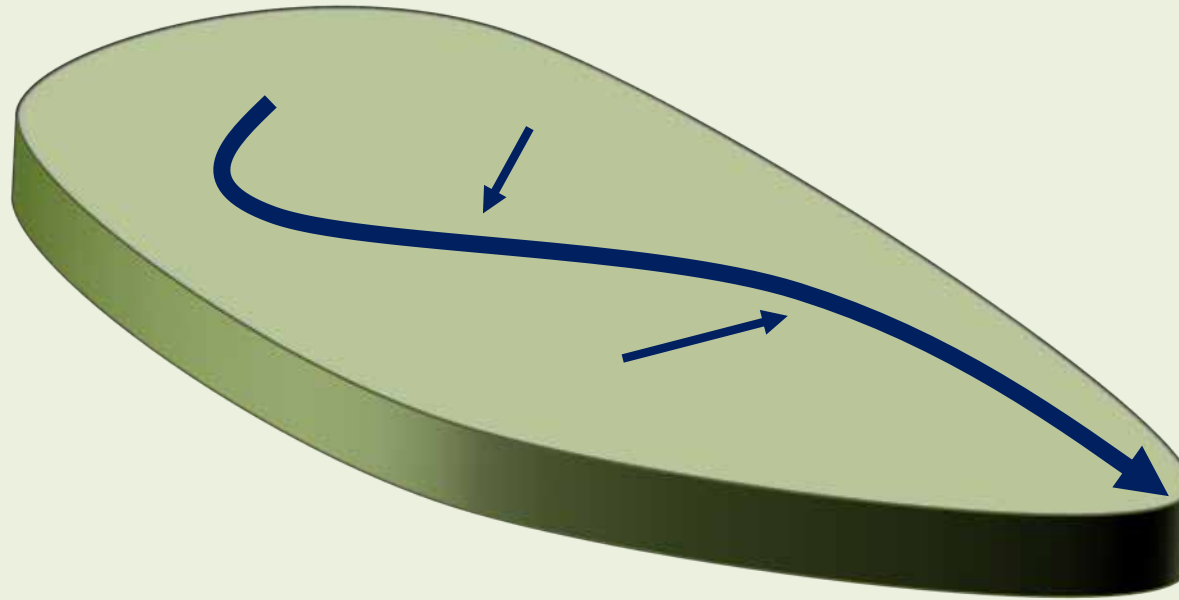
Today.... 1) Watersheds and 2) Lakes & 3) *Streams*

- **Functioning – big picture arm waving – & the development of “Conceptual” Models**
- **Modeling Approaches –**
 - **Fundamentals**
 - **Examples**

Goal- Understand & Apply several Models

(and most important... not make a potentially confusing topic more confusing...)

First, What's a Watershed?



Land area where the water drains to the outlet point of interest

Why is that important?





- Precipitation

___ Inches per Year +/-



___ storms per year +/-



___ hours of precipitation (>trace)
per year +/-



- Precipitation

32 Inches per Year +/-



100 storms per year +/-

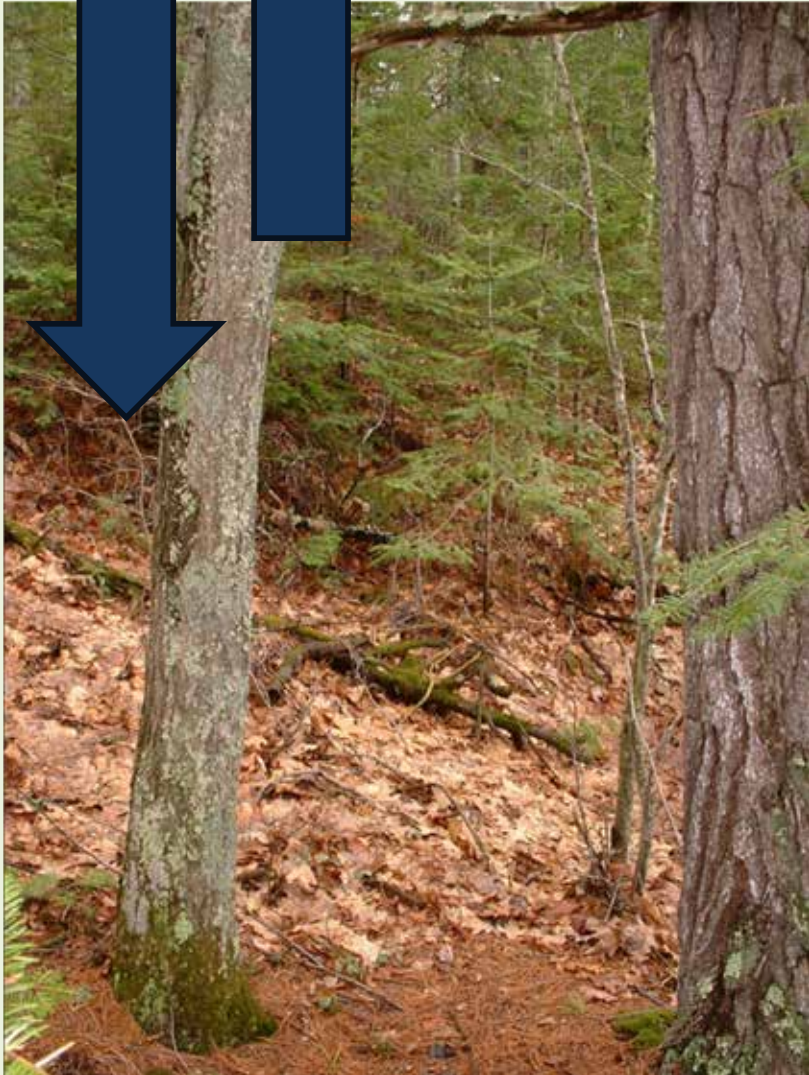


**500 hours of precipitation (>trace)
per year +/-**

Where does it go?

32"

22"



32"

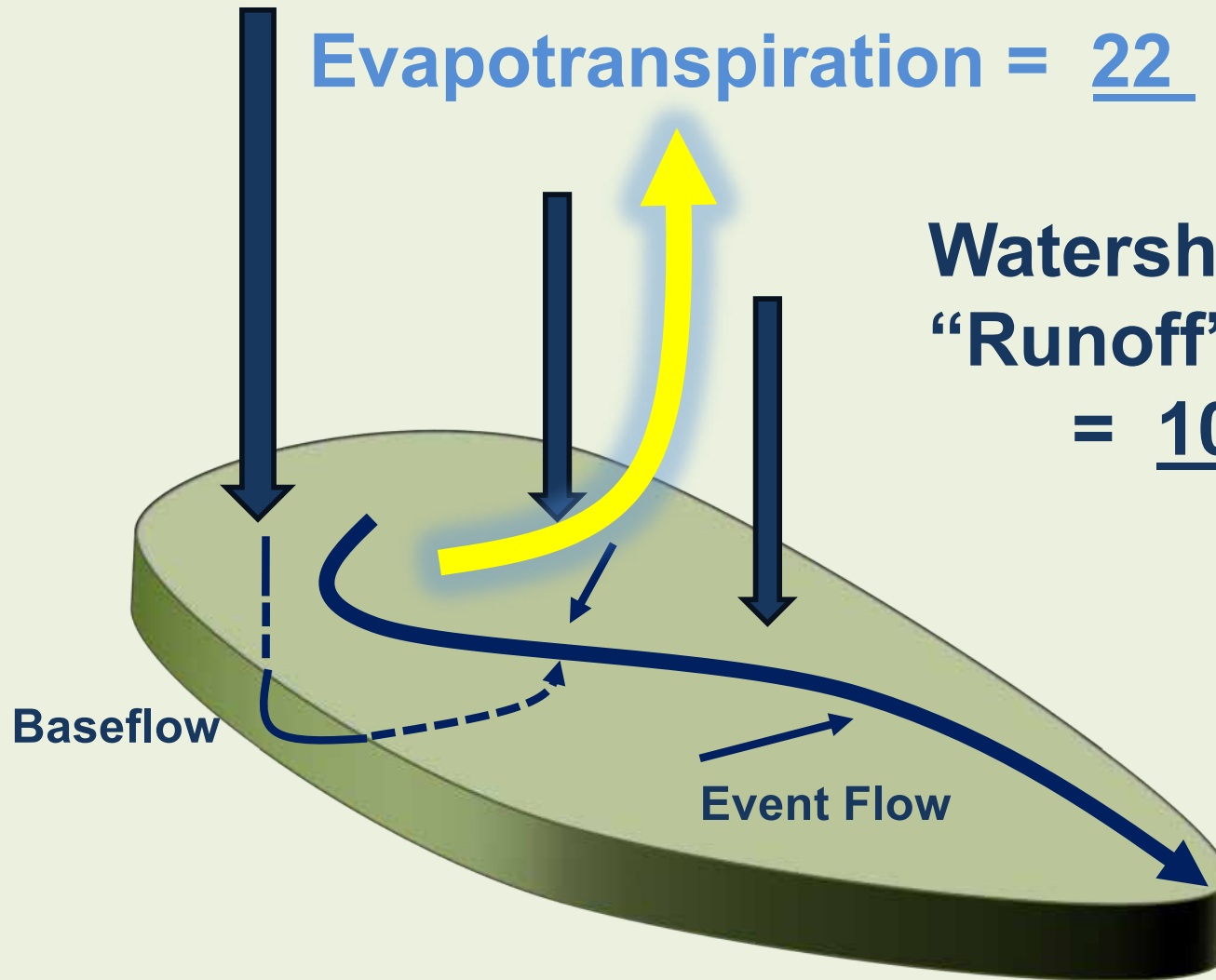
32"



Precipitation = 32 inches/yr

Evapotranspiration = 22 inches/yr

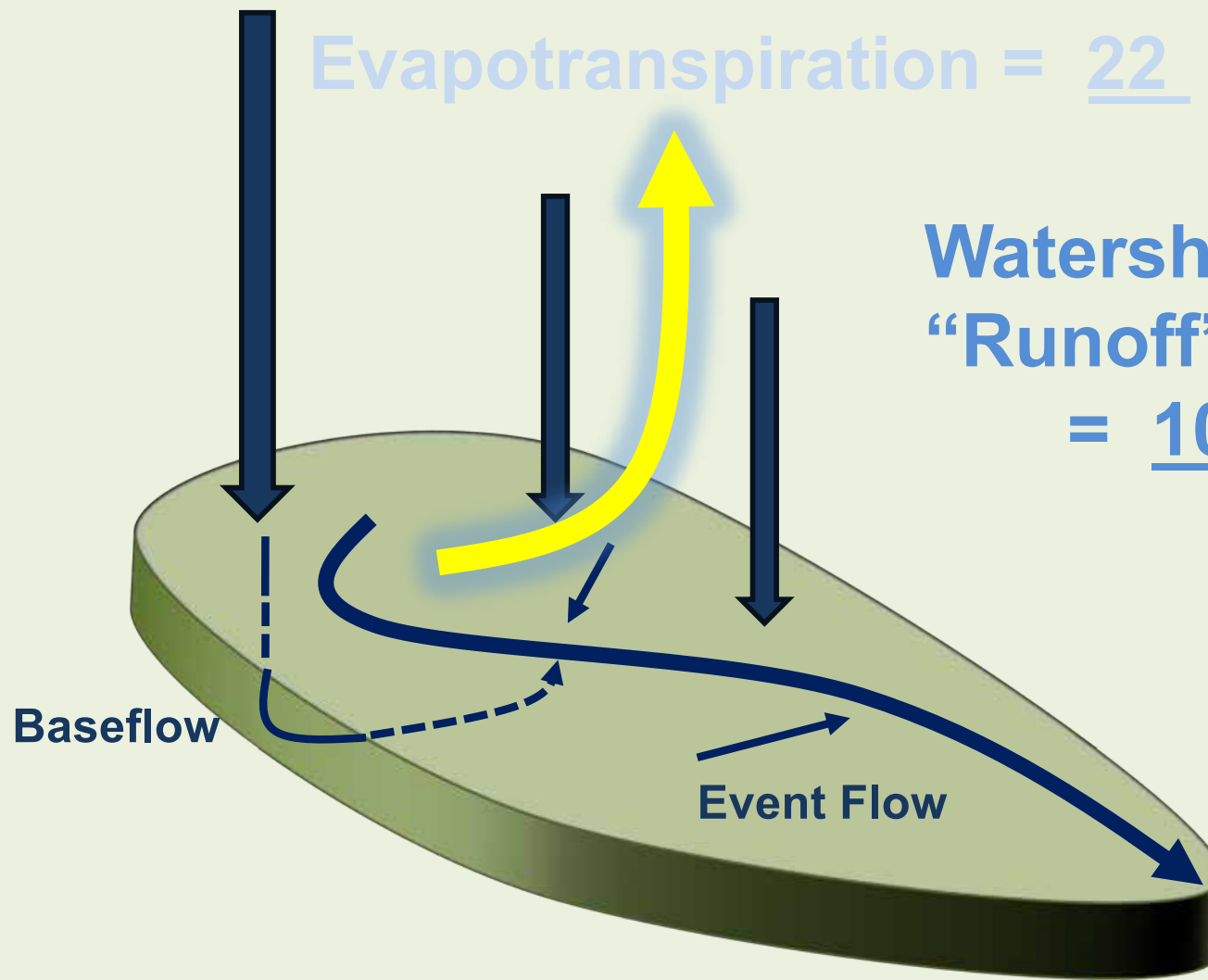
Watershed
"Runoff"
= 10 inches/yr



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Evapotranspiration = 22 inches/yr

Watershed
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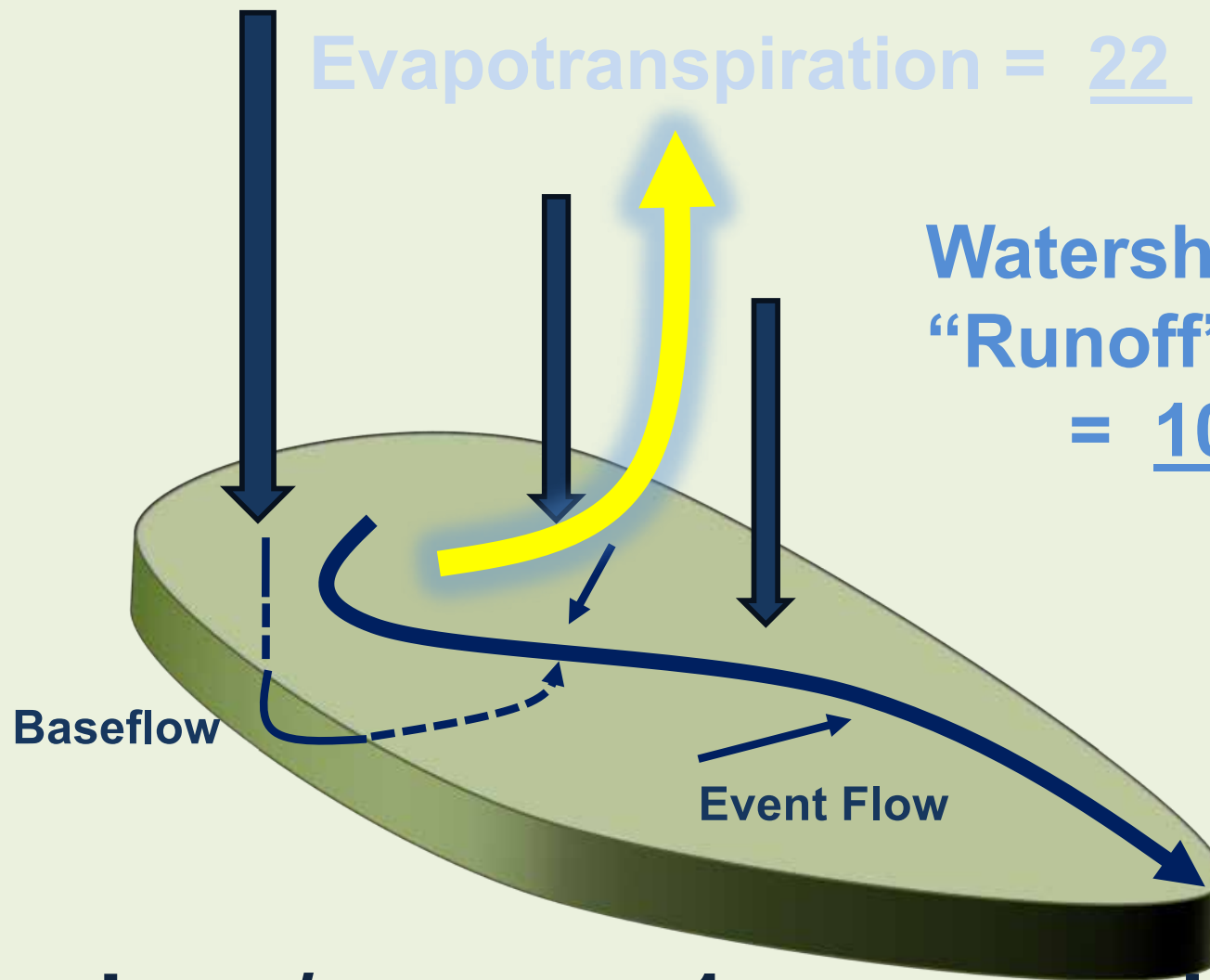


**10 inches /year on 1 square mile...
= 23,000,000 cubic feet /year!**

Precipitation = 32 inches/yr

Evapotranspiration = 22 inches/yr

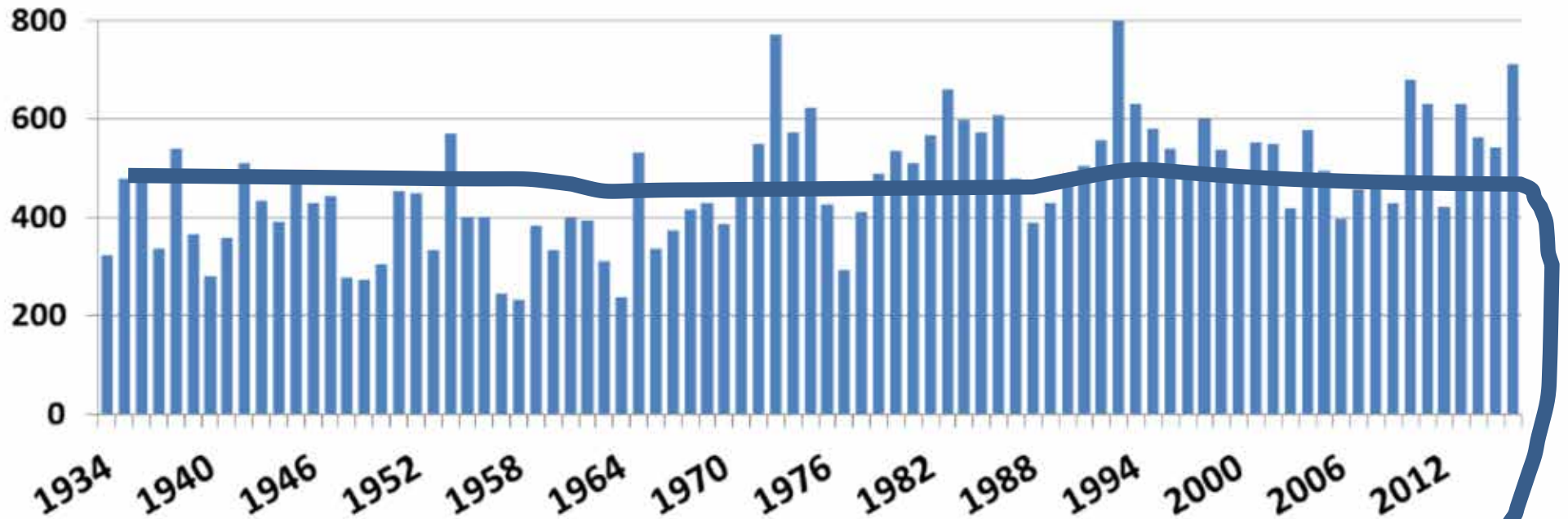
Watershed
"Runoff"
= 10 inches/yr



**10 inches /year on 1 square mile...
= 23,000,000 cubic feet /year!
= 0.7 cubic foot every second!**

Really?

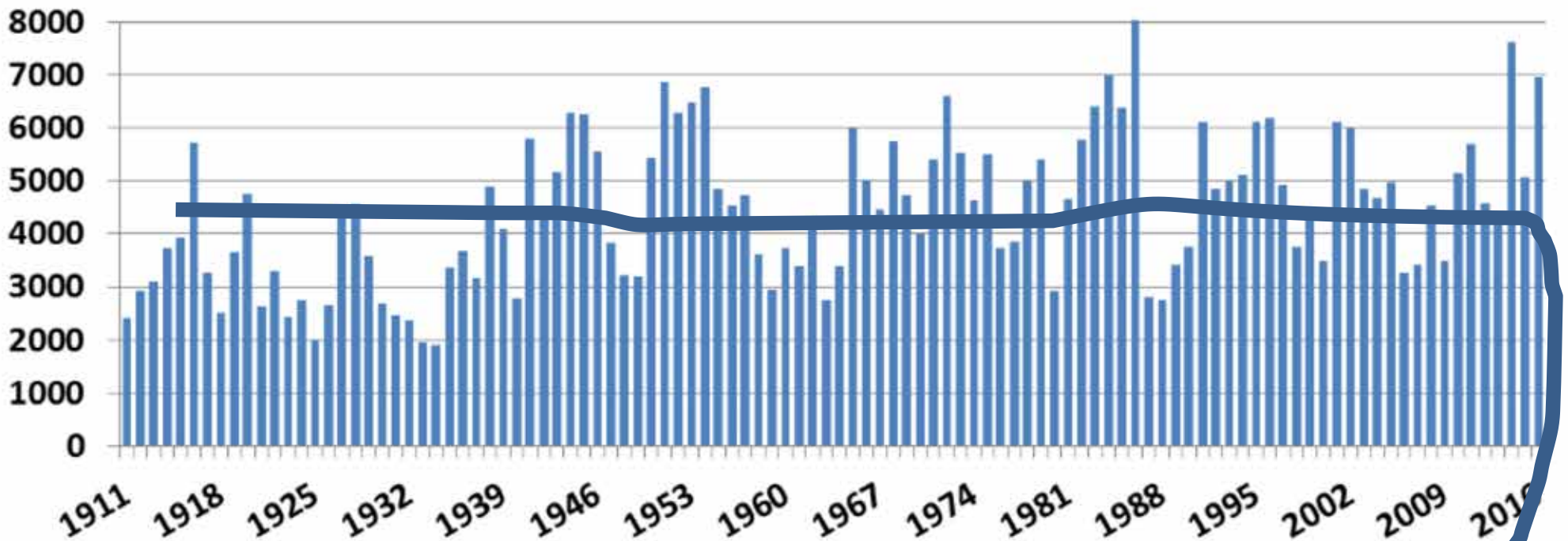
- **USGS 05379500 TREMPEALEAU RIVER AT DODGE, WI**
- **DRAINAGE AREA.--643 square miles.**



Average flow ~470 cubic feet per second

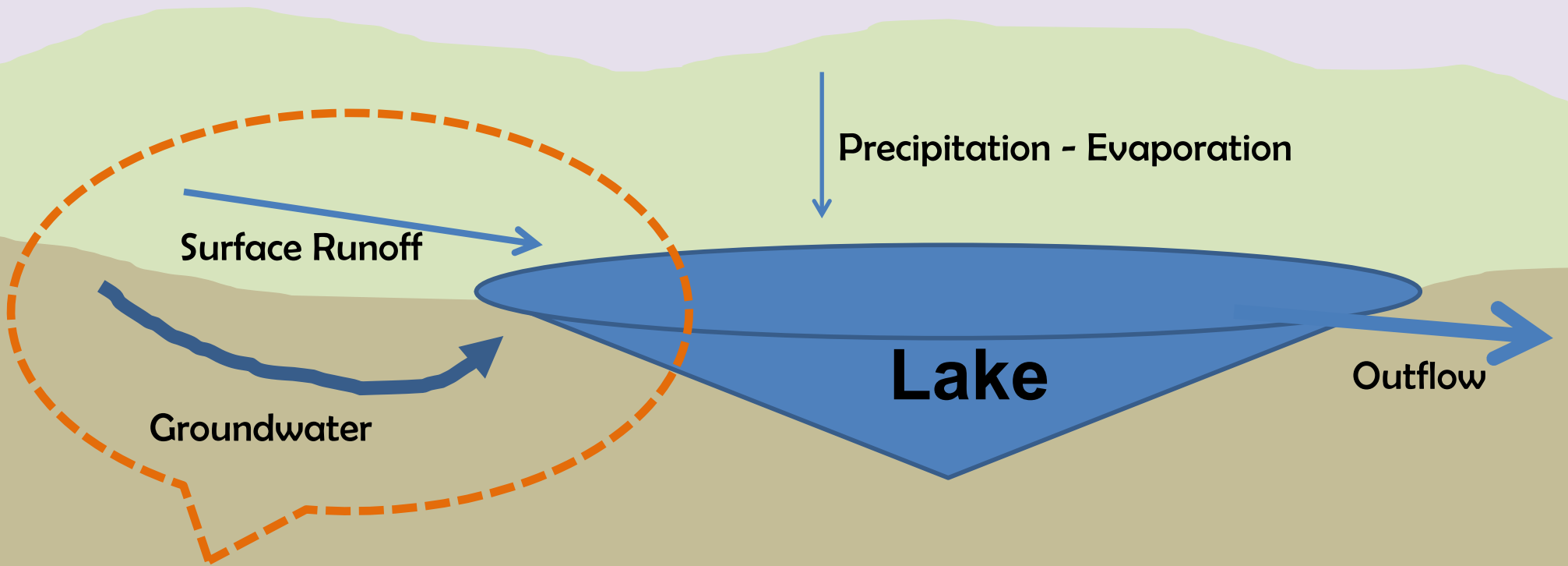
Really?

- **USGS 05340500 ST. CROIX RIVER AT ST. CROIX FALLS, WI**
- **DRAINAGE AREA.**—6,240 square miles.



Average flow ~4,432 cubic feet per second

This is a watershed model !



- Water Budget

Water Entering the Lake Each Year = (10 in/year)*(Watershed Area)

What's a model

One definition: A mathematical description to help visualize something

*help us “visualize” how a current condition
or help us “visualize” how future actions could
alter the current condition*

- Examples
 - How long does water spend in my lake?
 - If a wooded area is converted to row crops, what might that do to the phosphorus concentration in the lake?

- **Useful?**

- **Residence time =**

- =**
$$\frac{\text{Amount of Water in Lake}}{\text{Rate Which Water Leaves Lake}}$$

- **Useful?**

- Say 10,000 acre lake, mean depth of 40 feet with a 150,000 acre watershed

- Residence time estimate =

$$= \frac{(10,000 \text{ acre})(40 \text{ feet mean depth})}{(150,000 \text{ acre})(0.83 \text{ ft/yr})}$$

$$= 3.2 \text{ years}$$

Rule #1

“All models are wrong but some are useful”

George Box



Limitations

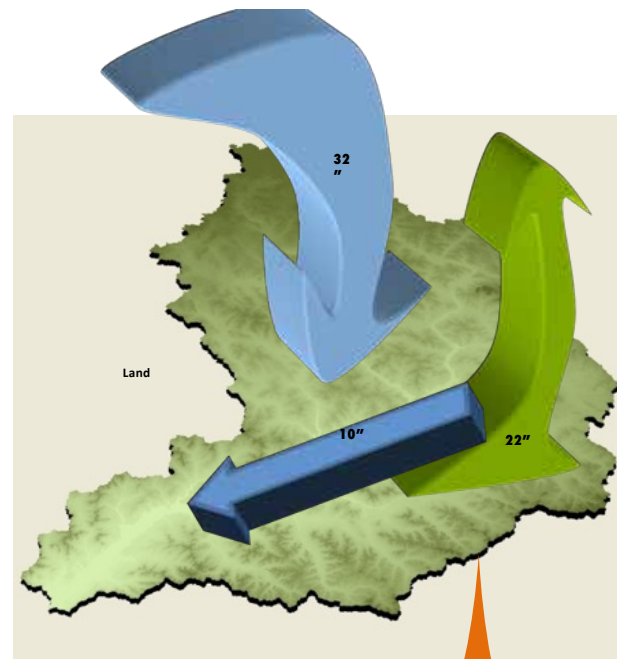
- Year-to-Year Variations?
- Different parts of the watershed have different response
 - Impervious surfaces
 - Compacted soil / raindrop impact

How can we improve this model?

- Spatial Variability
- Temporal Variability

- Of course this comes at a cost... is it necessary? Is it worth it?

Modeling the Land?



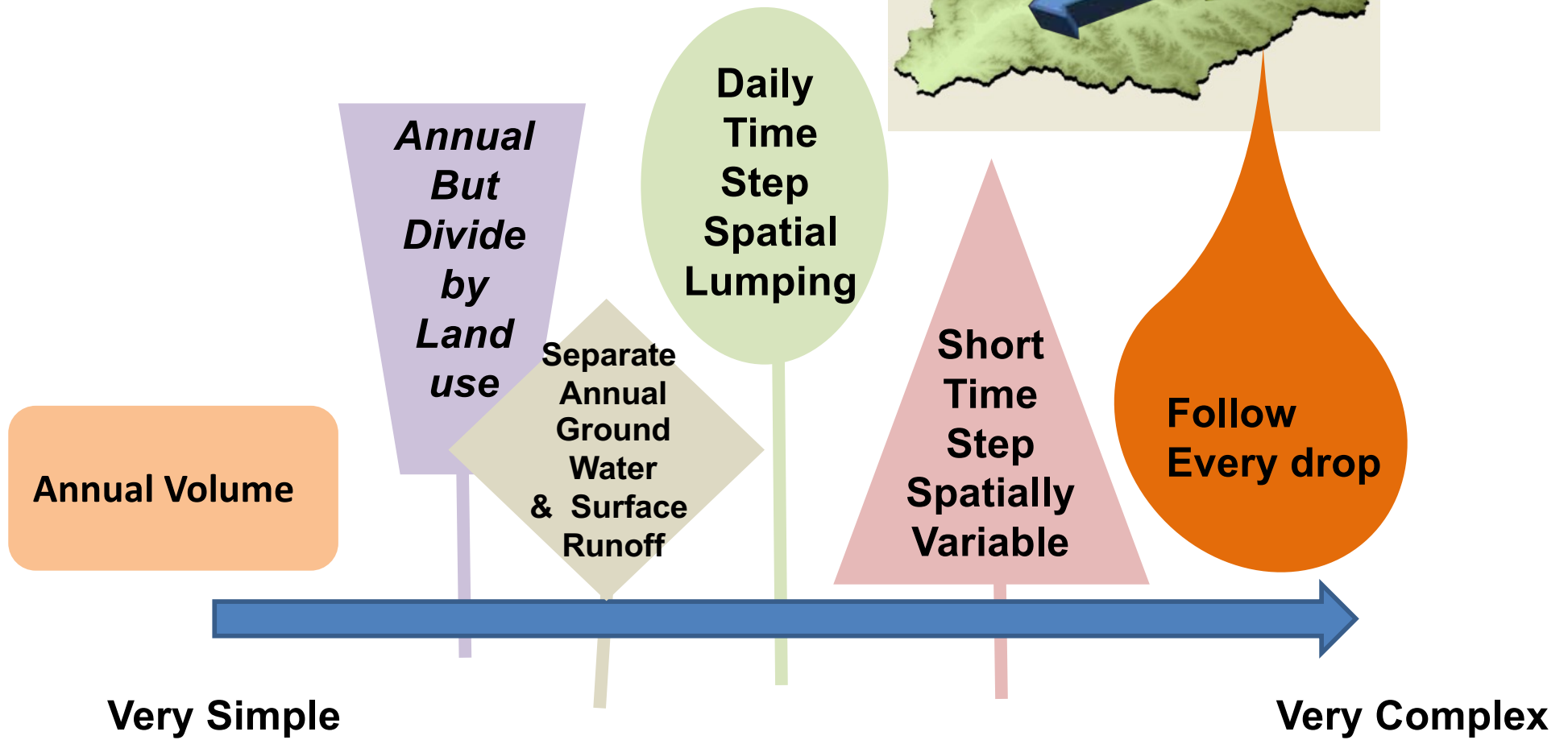
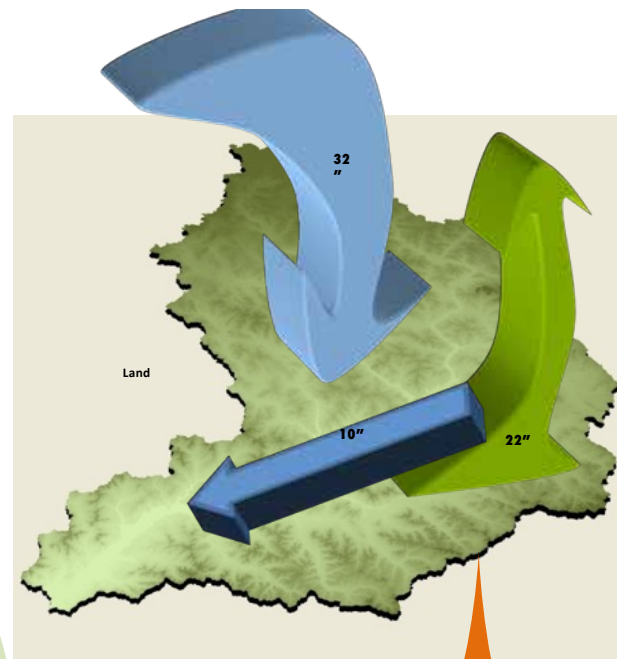
Annual Volume

Follow
Every drop

Very Simple

Very Complex

Modeling the Water on Land?



Closely Related...**Nutrient Movement**

- Just talked about water movement on land
- Next... **Nutrients Loss from Land**
–then **Lakes & Streams**

Let's look at Phosphorus Movement

- Important Implications for Lakes & Streams
- Oligotrophic - “few” “foods”
- Eutrophic – “many” “foods”

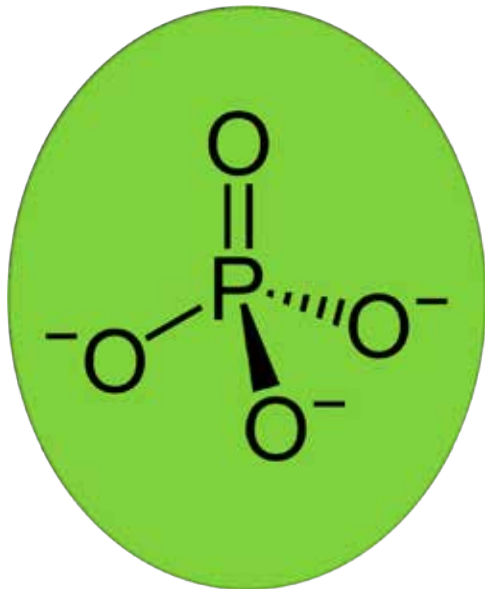
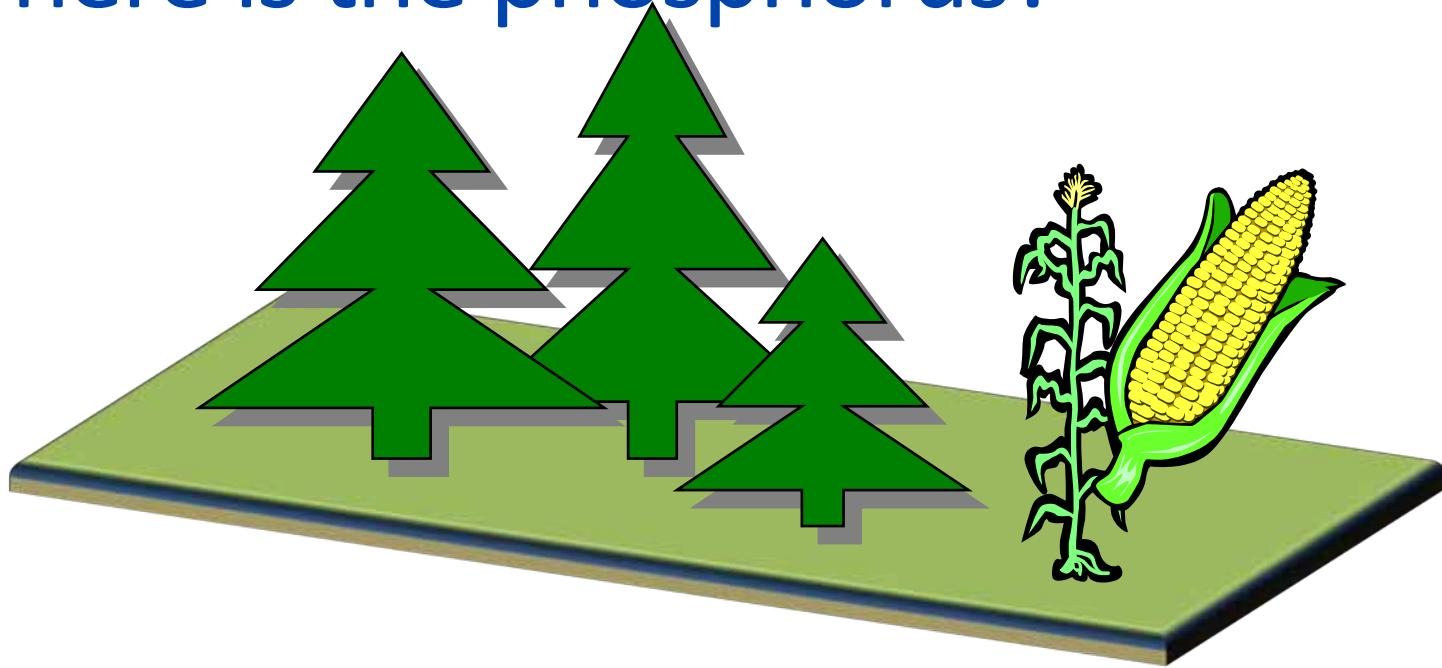


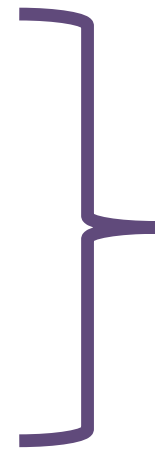
Table 1. Completed trophic state index and its associated parameters.

TSI	Secchi disk (m)	Surface phosphorus (mg/m ³)	Surface chlorophyll (mg/m ³)
0	64	0.75	0.04
10	32	1.5	0.12
20	16	3	0.34
30	8	6	0.94
40	4	12	2.6
50	2	24	6.4
60	1	48	20
70	0.5	96	56
80	0.25	192	154
90	0.12	384	427
100	0.062	768	1183

Where is the phosphorus?



45,000 lb plant P
50,000 lb organic matter P
250,000 lbs soil P (top 6")



350,000
lb P
/sq mile

- Water Across Land = Phosphorus in the Water



Tale of Two Pathways

10 inch/year @
0.02 mg/l <
0.01
lb/acre /year

2 inch/year @ 1
mg/l = 0.45
lb/acre
/year

(+ 9 inch/yr @
0.02 mg/l)

“Phosphorus Export Coefficients” (pounds/acre-year)

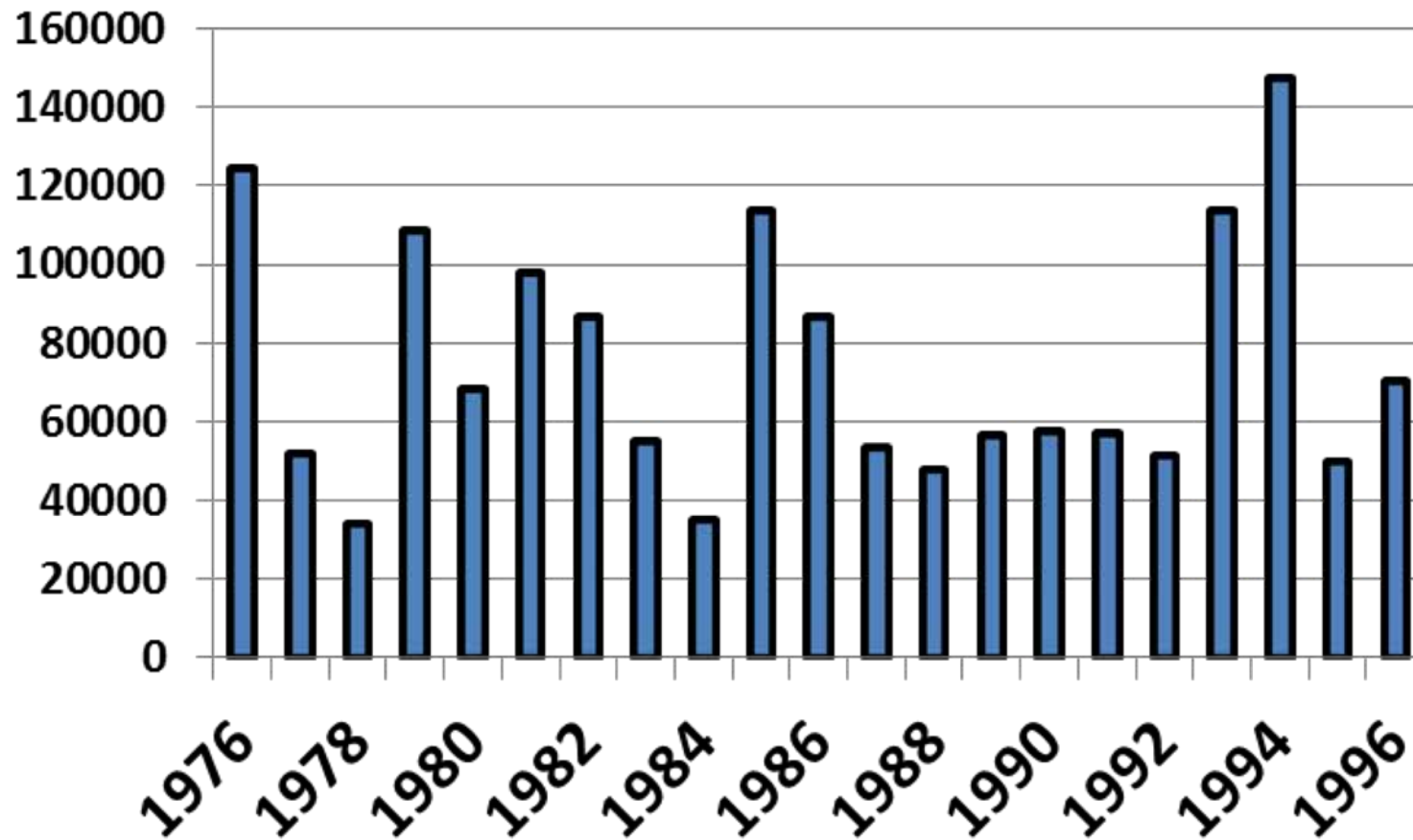
	Low	Most Likely	High
Agriculture (Mixed)	0.3	0.8	1.4
Med Density Urban	0.3	0.5	0.8
Pasture	0.1	0.3	0.5
Forest	0.05	0.09	0.18
Atmospheric (lake surface)	0.1	0.3	0.5

Adapted from WiLMS, Wisconsin Lake Modeling Suite
<http://dnr.wi.gov/lakes/model/>

Useful?

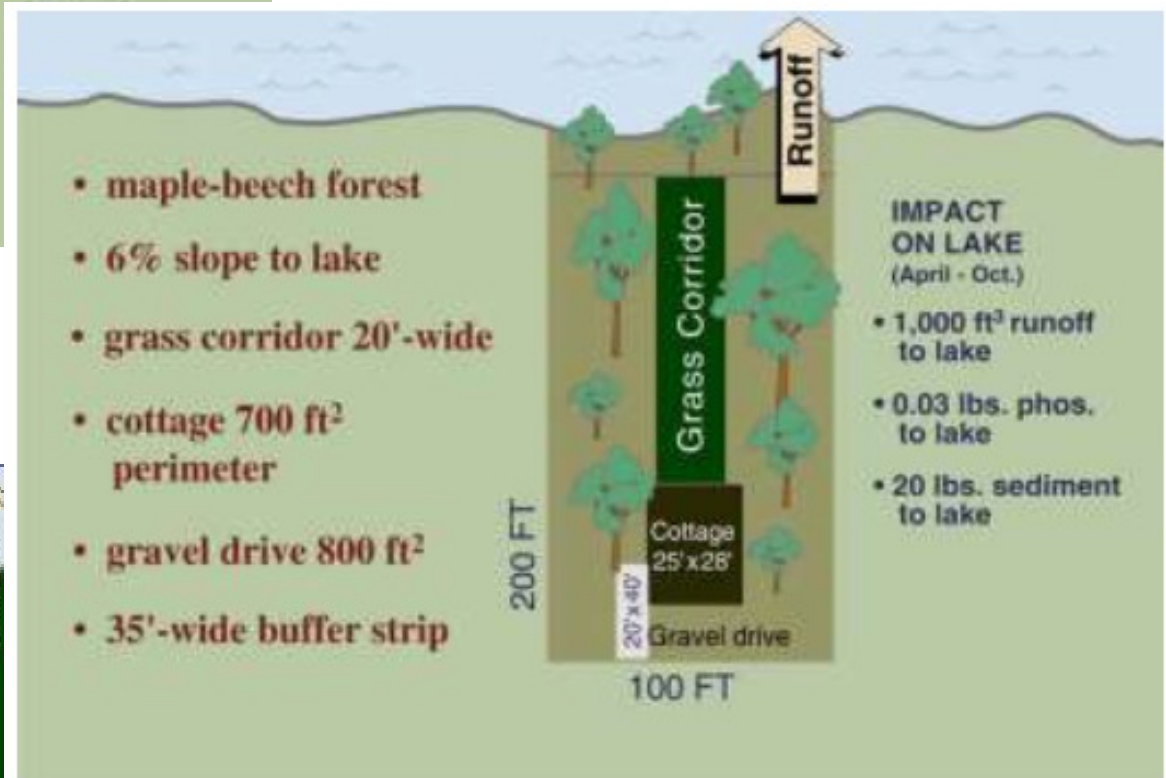
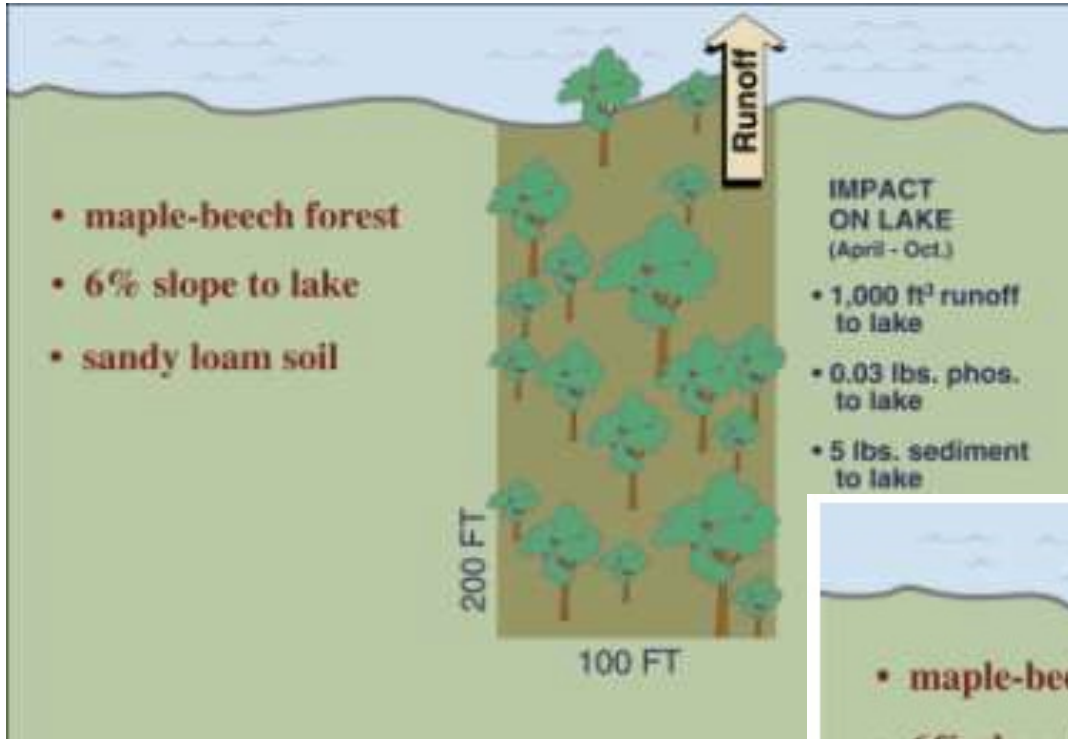
- Estimate the long term average P transfer from a watershed to the lake
 - 90,000 acres Row Crop
 - $90,000 \text{ ac} * 0.8 \text{ lb/ac-year} = 72,000 \text{ lbs/year}$
 - 30,000 acres Pasture/Grass
 - $30,000 \text{ ac} * 0.3 \text{ lb/ac-year} = 9,000 \text{ lbs/year}$
 - 30,000 acres Med Den Urban
 - $30,000 \text{ ac} * 0.5 \text{ lb/ac-year} = 15,000 \text{ lbs/year}$
 - TOTAL = 96,000 lbs/year

Challenges: Annual Variations in P to Lake!

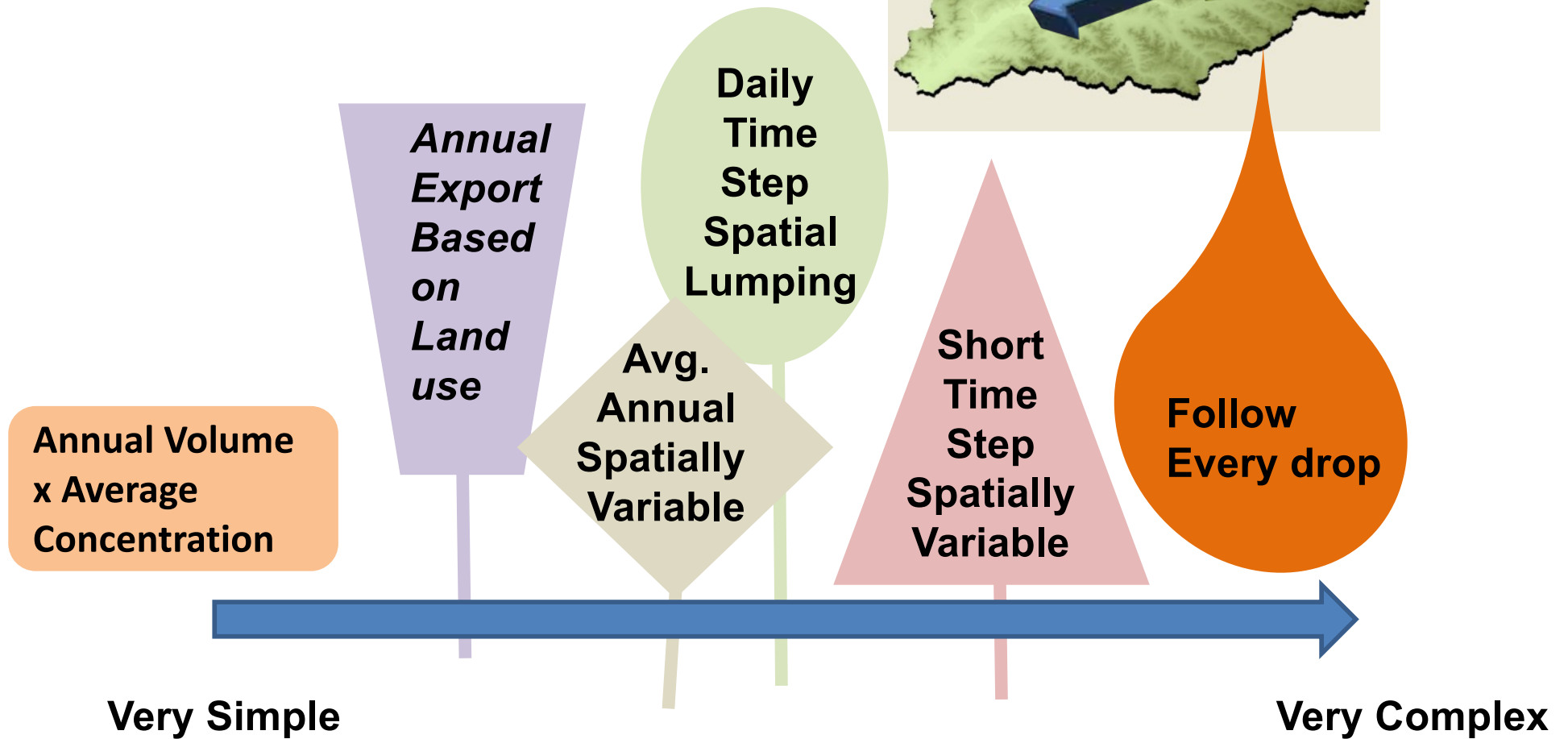
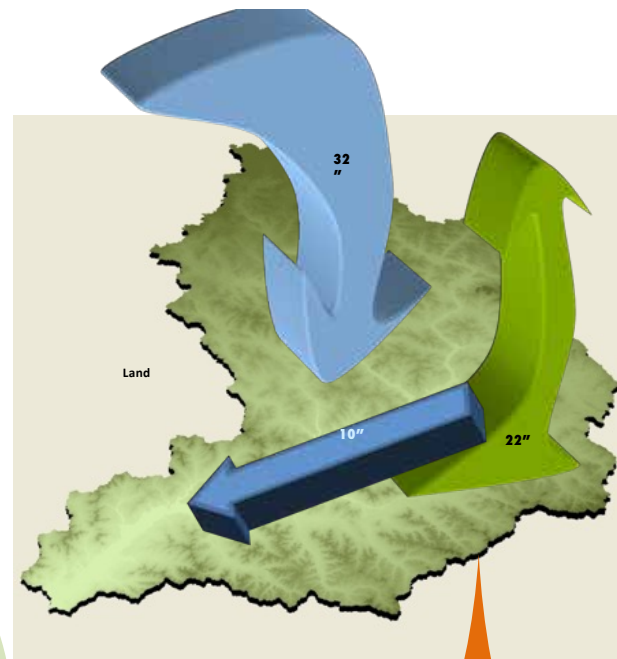


- P Load (lb) to Lake (Lathrop and Panuska)

Development



Modeling the Land?

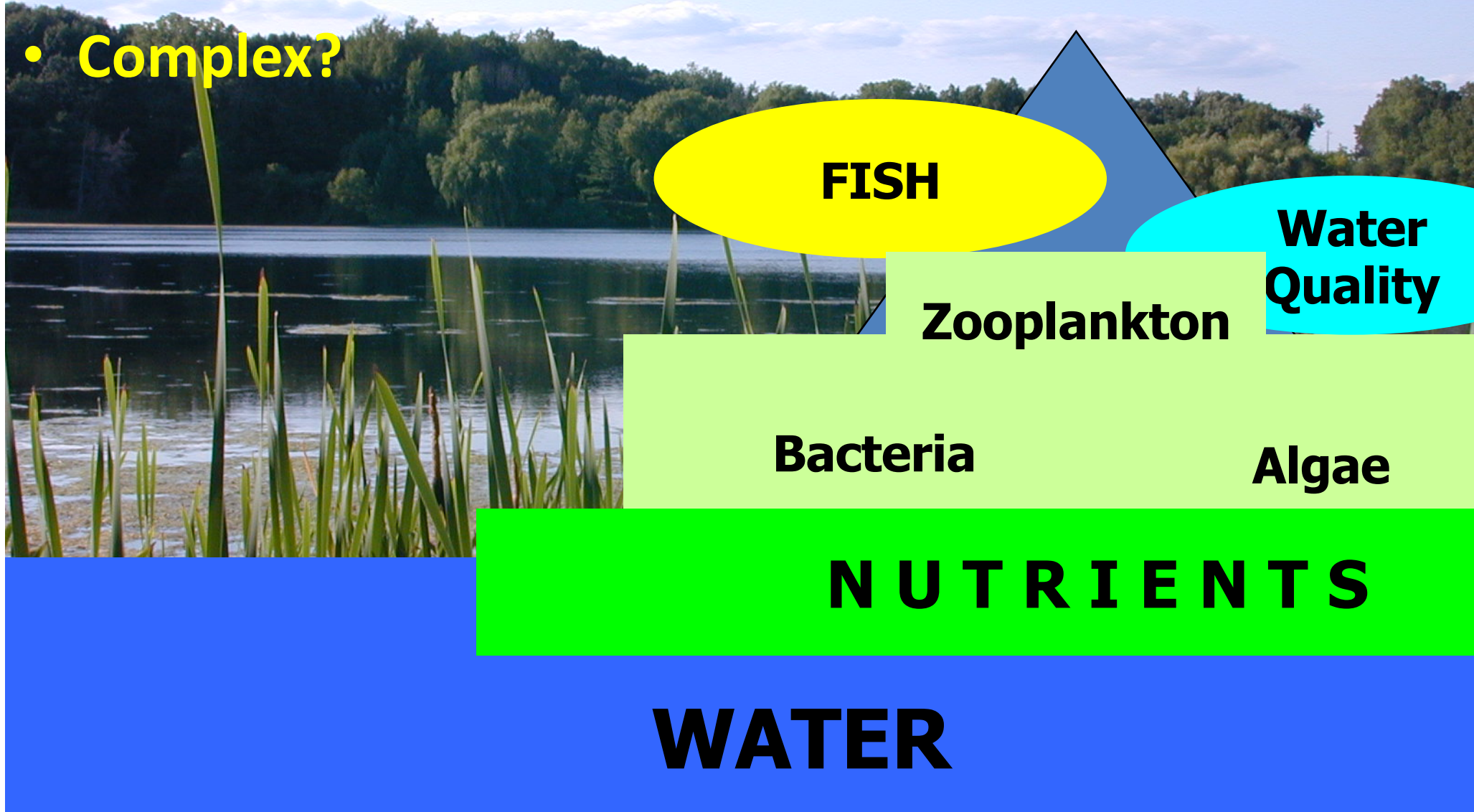


Part 2 - LAKES



- Important
- But what do we want to model?
 - Water level, Algal density, Fish, Phosphorus Concentration

- **Complex?**

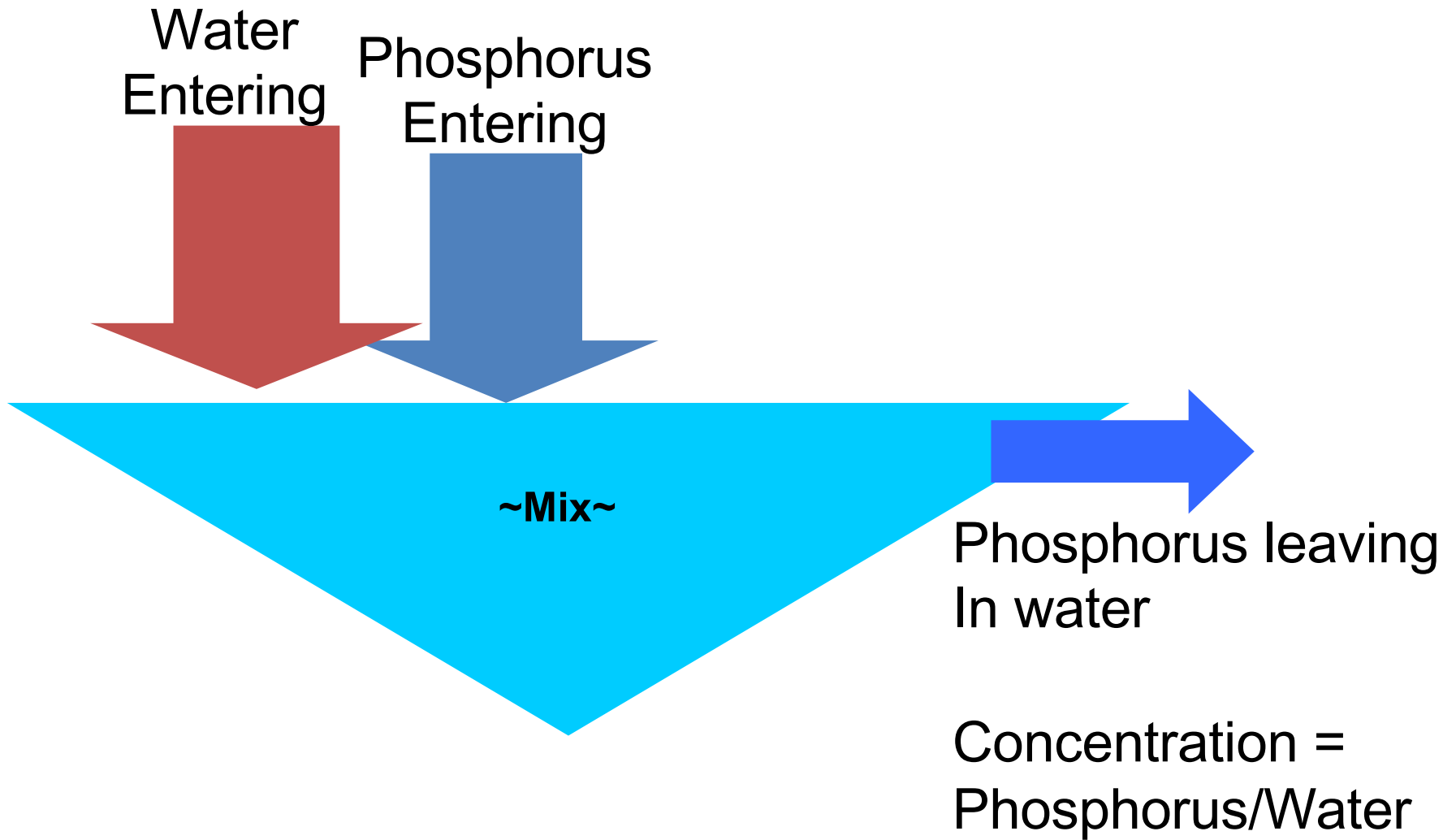


Our First Model

- Goal– predict the P concentration

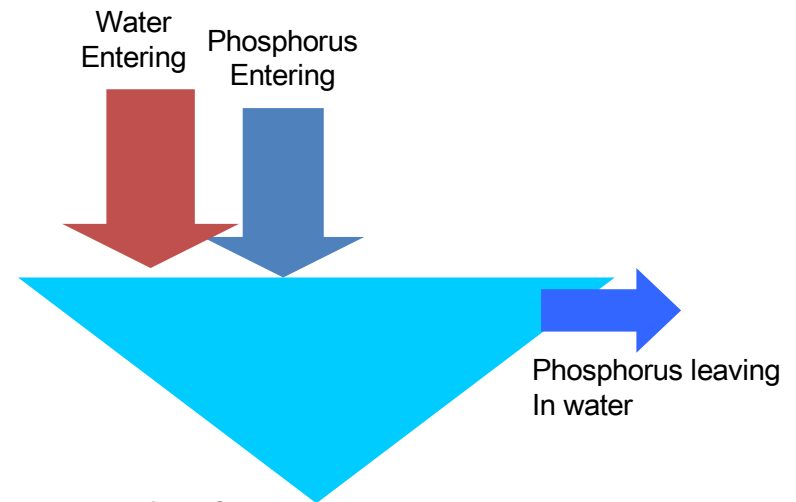
Given

- The amount of P entering the lake
- The amount of water entering the lake



Let's give this a try

- 10,000 acre lake
- 150,000 acre watershed



Recall our simple watershed model...

- 96,000 lb/year P
- 125,000 acre-ft/year water

“Simple Model” (annual P/annual water)

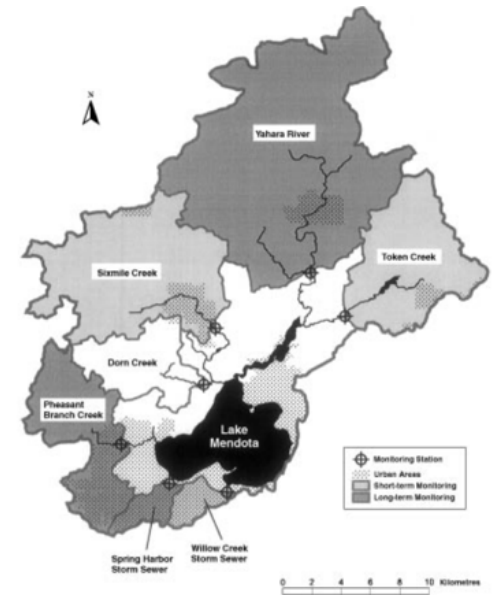
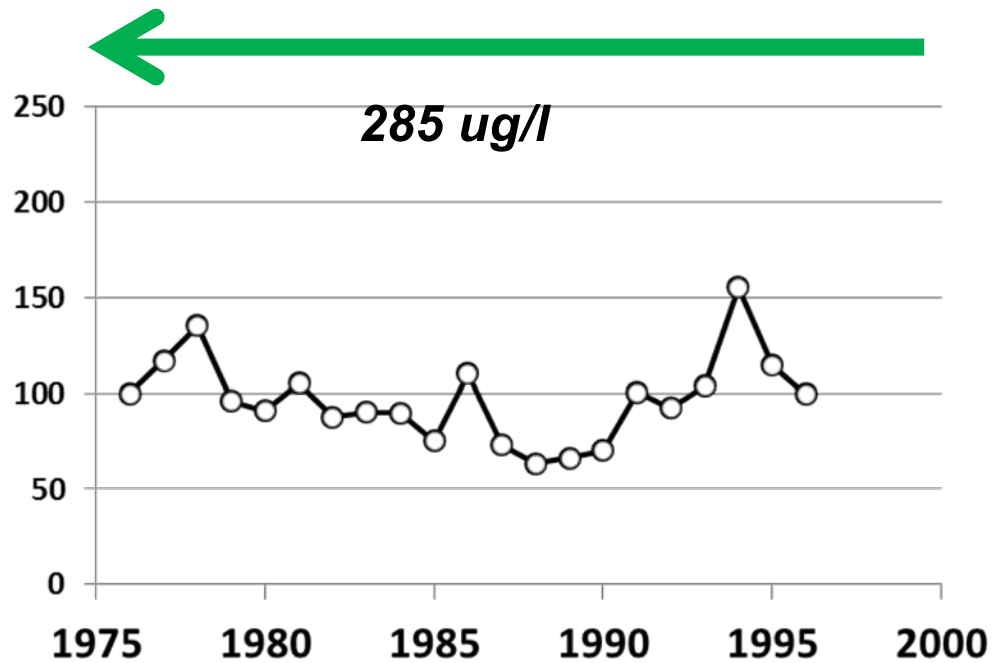
- *Concentration of P*

= Mass of P / Volume of Water

= 96,000 pounds / 23,000,000 cubic feet

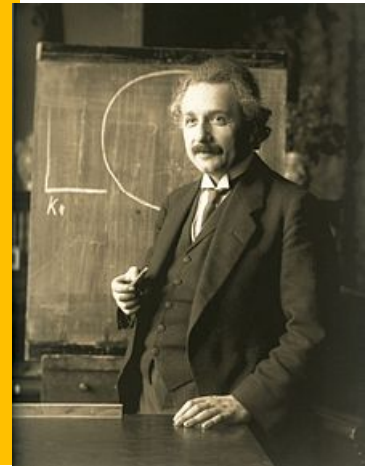
= 285 ug/l

Take a look at some data

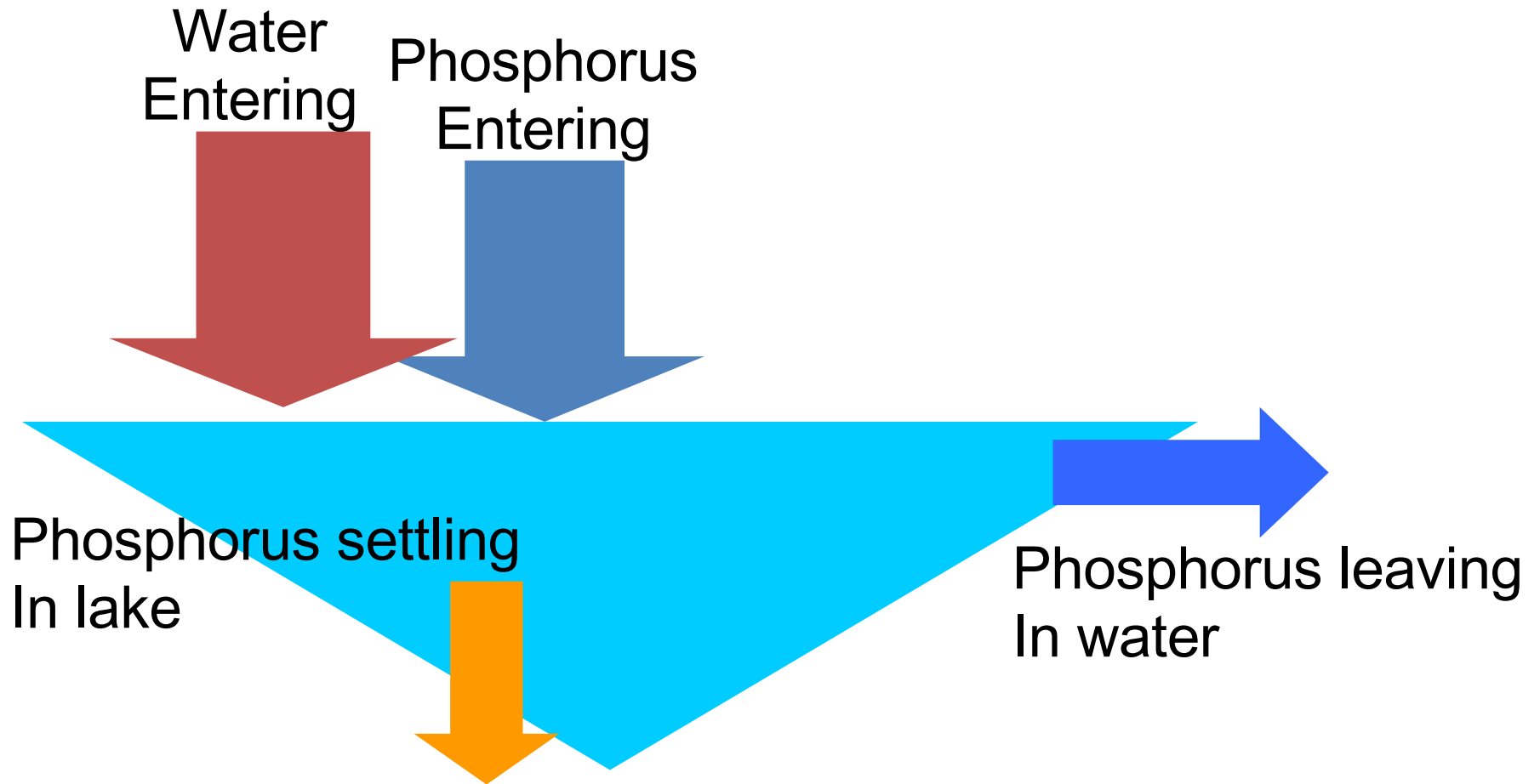


Not a very good model

- Why?
- What happens to P in a lake?
- Another observation on modeling
 - “Everything should be made as simple as possible, but no simpler” A. Einstein



Second Model



“diminished by retention term as P apparently lost to sediments” (Nurnberg, 1984)

Uniform (“steady-state”) Conditions

The P concentration doesn't change with time

The amount of P in the lake is constant

Phosphorus Concentration in Lake

Mass of Phosphorus per year entering lake

$$C_P = \frac{M}{Q + vA}$$

Amount of water Entering lake in a year

*Settling term (“settling velocity” * Area)*

The diagram shows the equation $C_P = \frac{M}{Q + vA}$ with several blue arrows pointing to its components. An arrow from the text 'Phosphorus Concentration in Lake' points to C_P . An arrow from 'Mass of Phosphorus per year entering lake' points to M . An arrow from 'Amount of water Entering lake in a year' points to Q . An arrow from 'Settling term (“settling velocity” * Area)' points to vA . A grey arrow points from the text 'With this added' to the vA term.

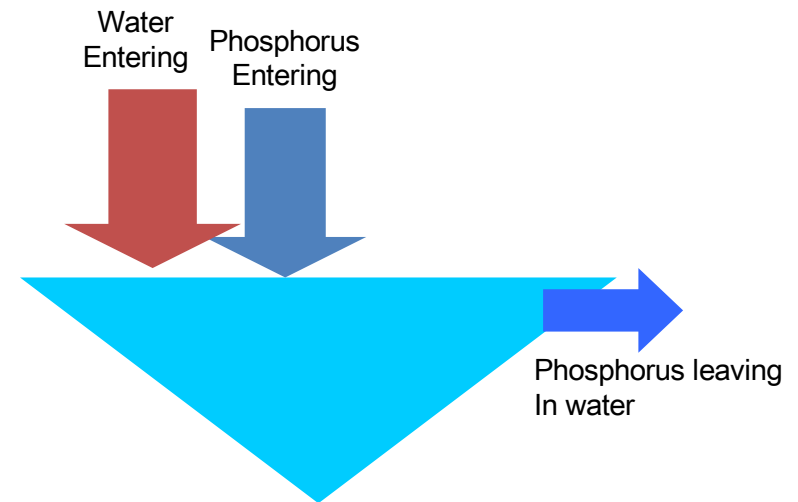
With this added

Let's give this a try

- 10,000 acre lake
- 150,000 acre watershed

Assume

- 96,000 lb/year P
- 125,000 acre-feet water/year
- 40,500,000 m² lake surface
- 10 meter/year settling velocity

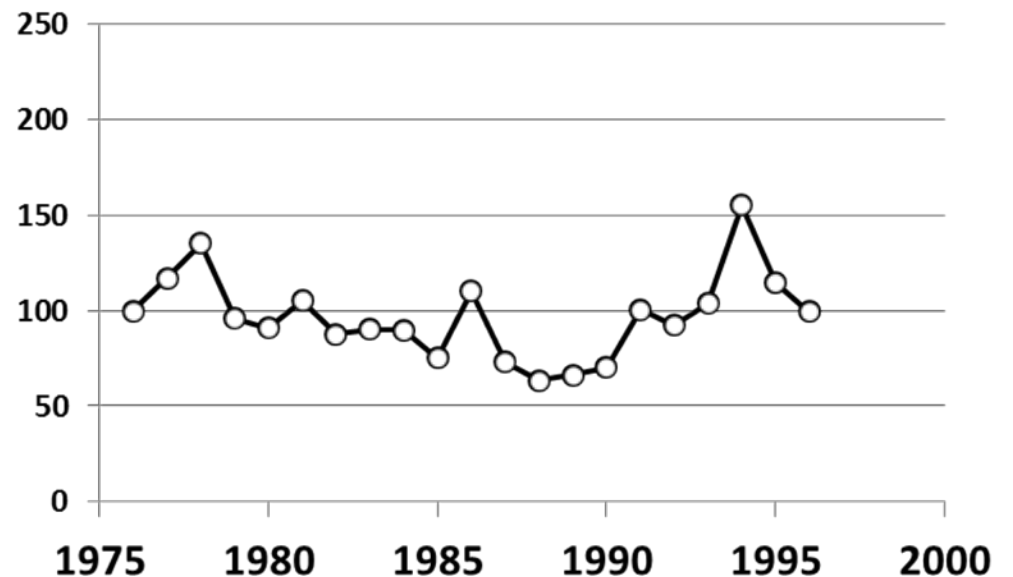


Our “Less Simple Model”

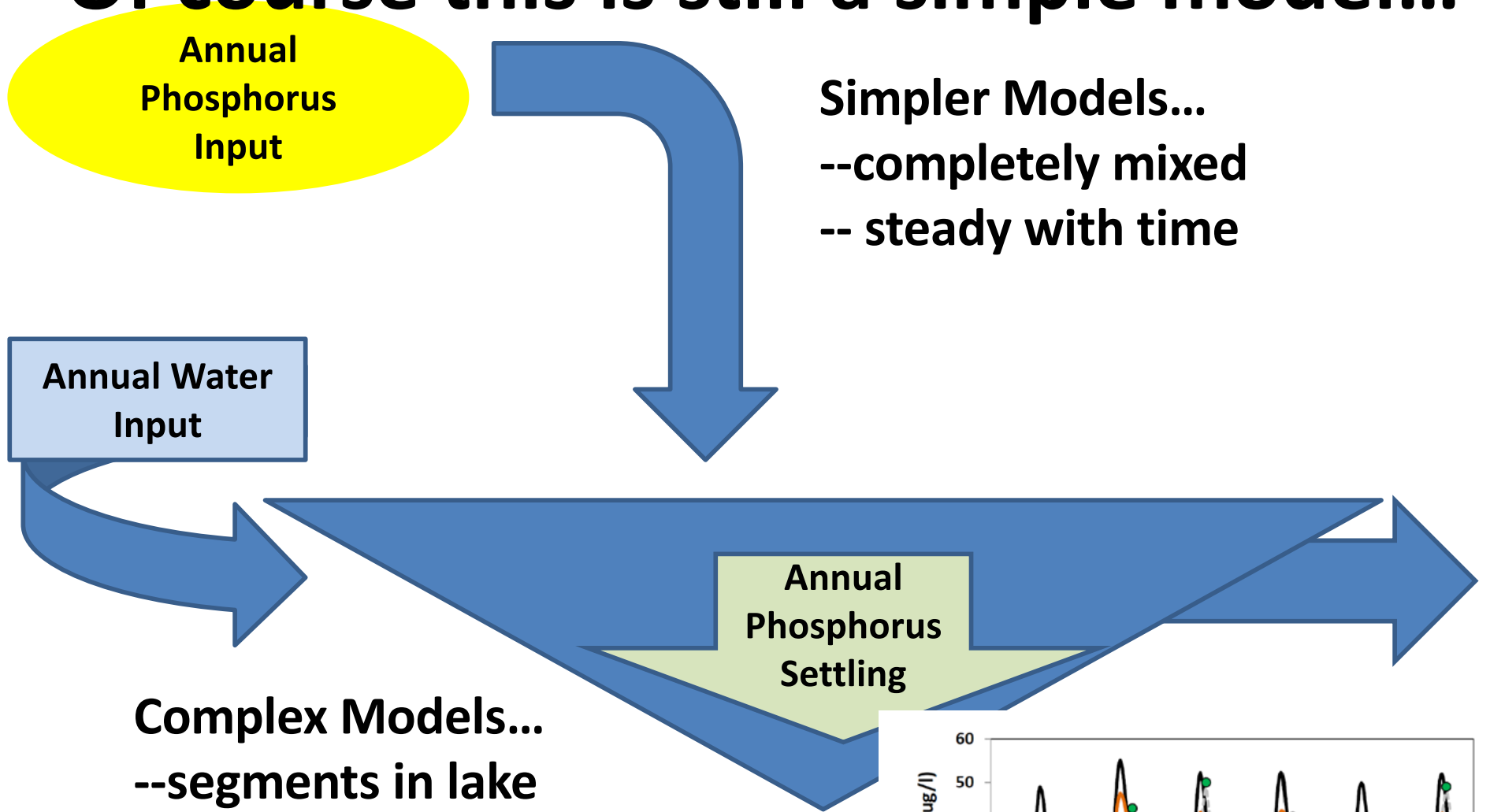
- Concentration of P

= 108 ug/l (better?)

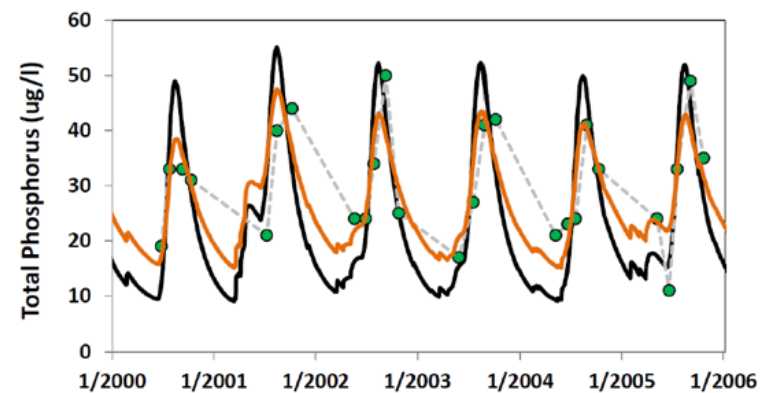
- Useful?



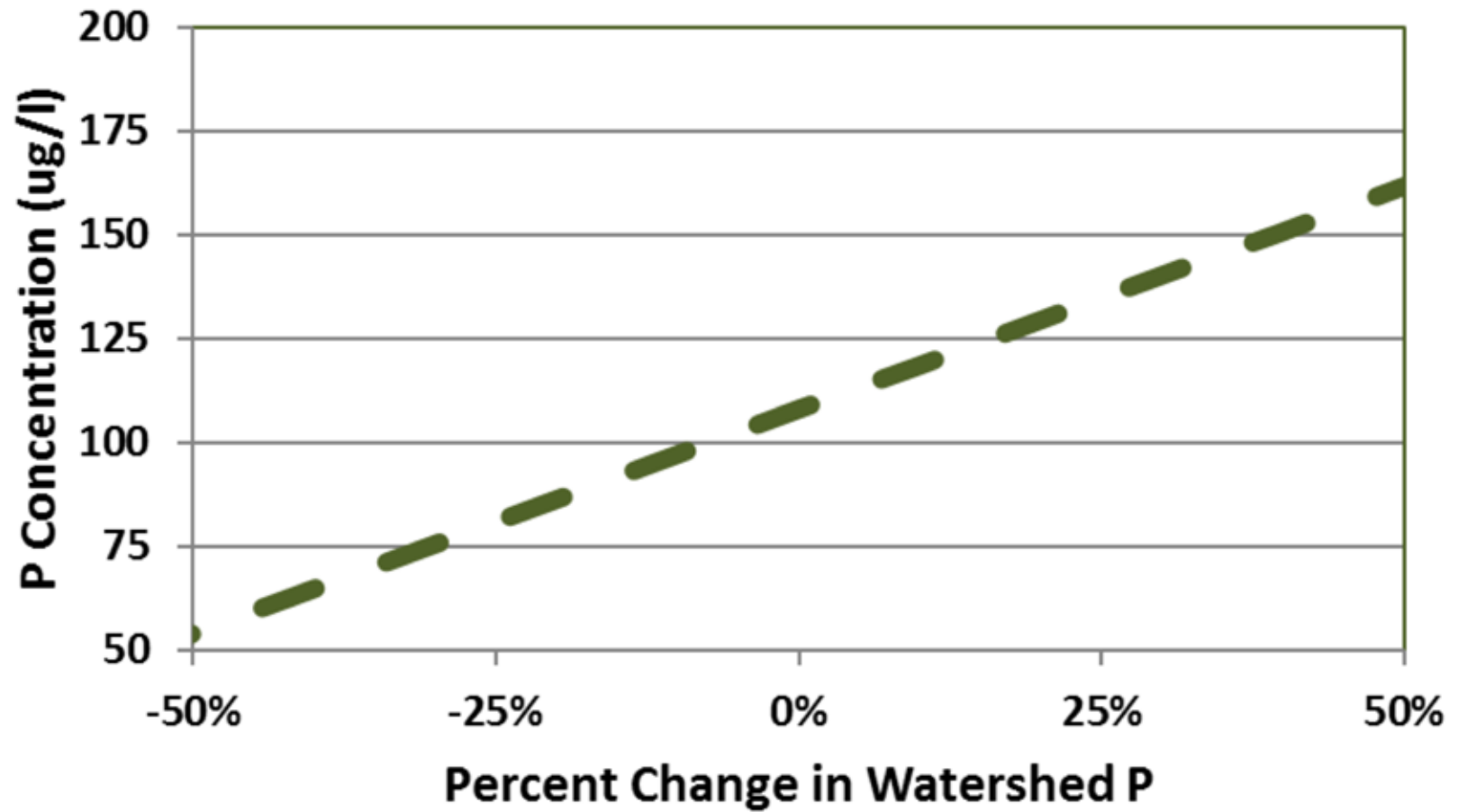
Of course this is still a simple model...



Complex Models...
--segments in lake
--vary with time
--biology!



Useful?



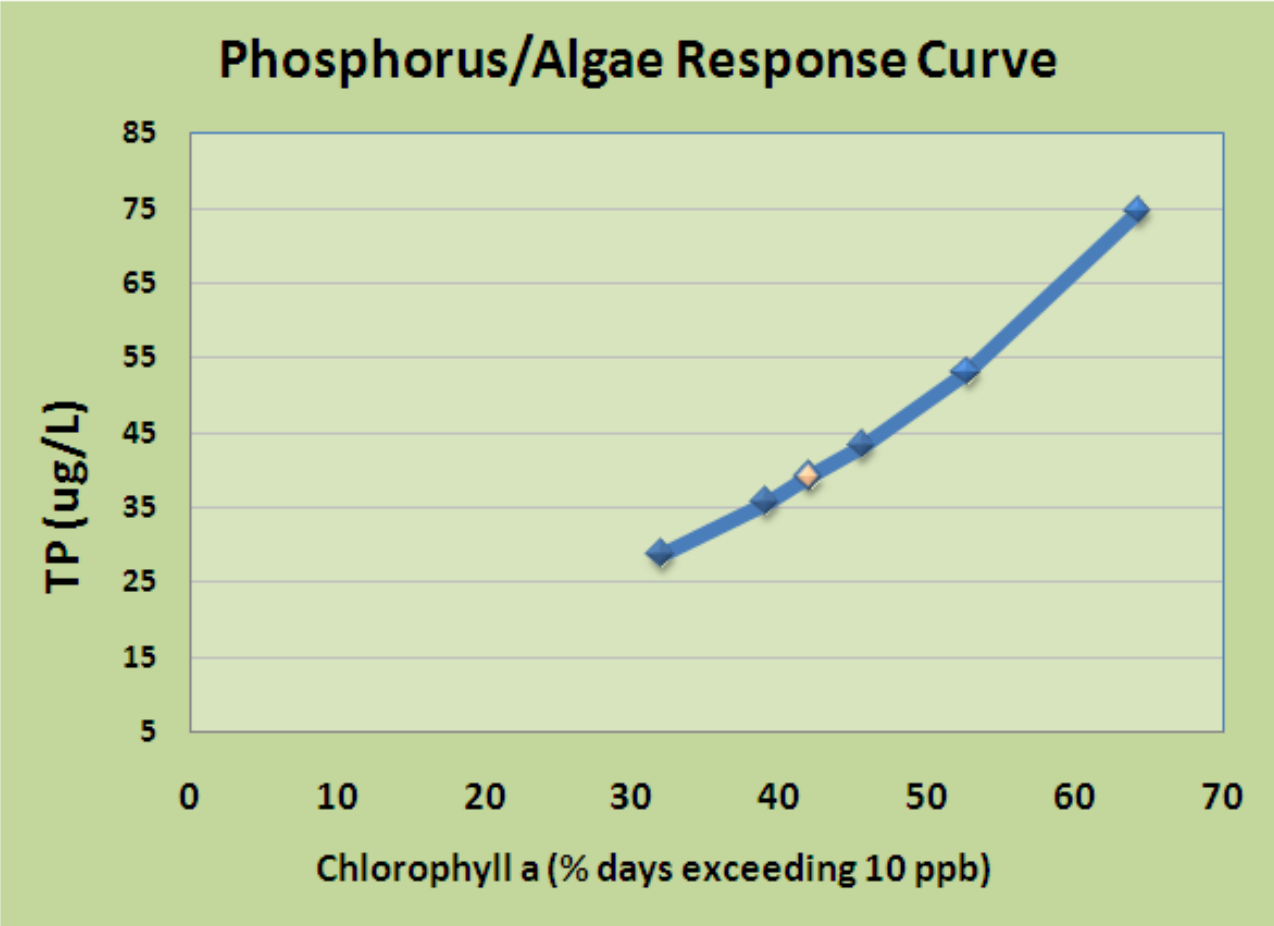
Lake Response Model?

Phosphorus
Concentration

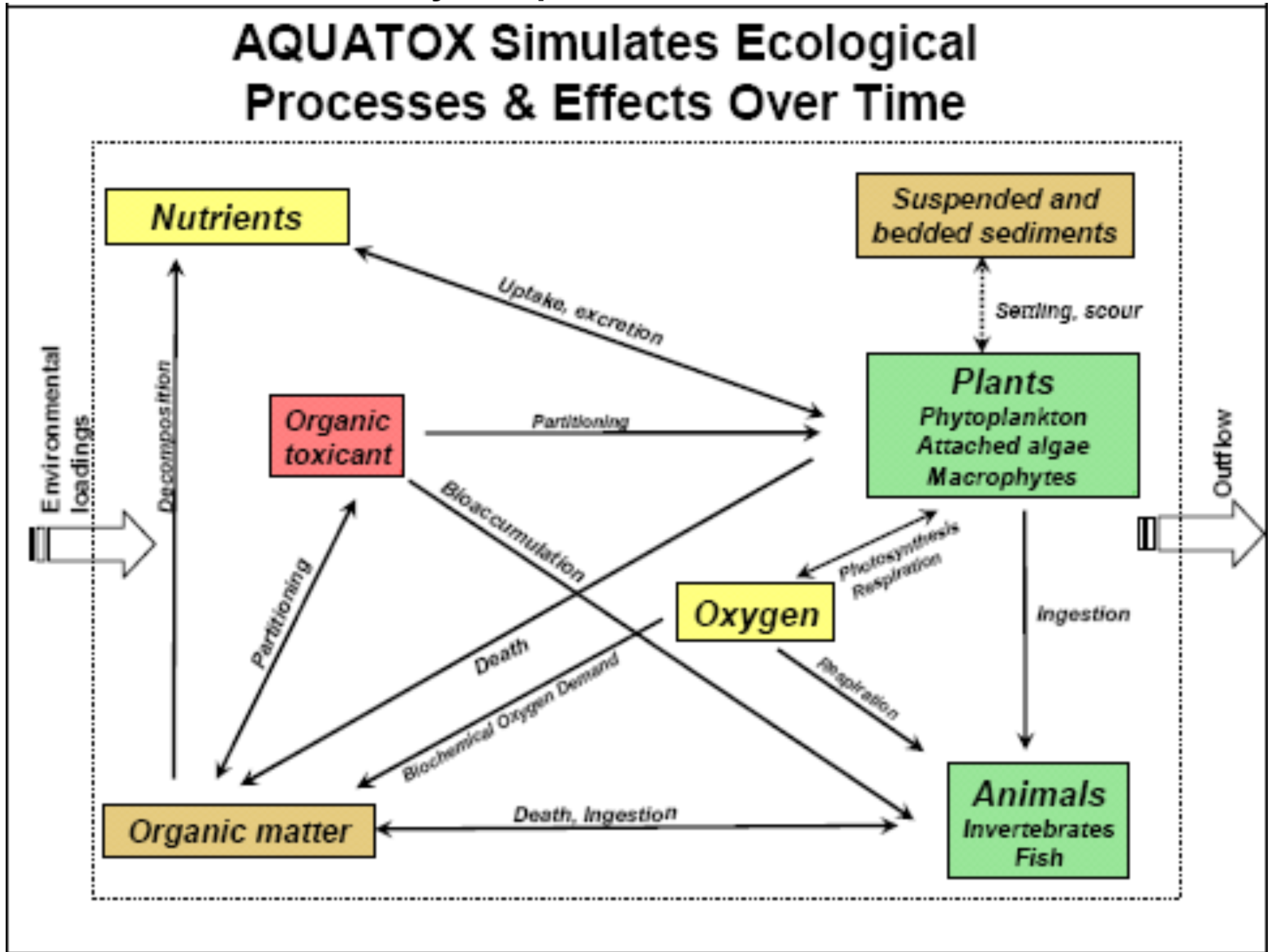
The diagram features a large blue inverted triangle representing a lake. Inside the triangle, on the left, is an orange oval containing the text 'Phosphorus Concentration'. A pink arrow points from this oval to a green rectangle on the right containing the text 'Algal Concentration'.

Algal
Concentration

- Useful?



But we can make this very complex!



Summary Discussion

- Watershed
 - Water Budget
 - Phosphorus Budget
- Lake
 - Concentrations
 - Response

- Simple
 - Reduce Spatial Variations
 - Long Term Averages
- Complex
 - Time and Space Variations
 - Daily / Yearly Variations

Questions

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